

1) $\sqrt{4x-9} = 6$
 $4x-9 = 36$
 $4x = 45$
 $x = \frac{45}{4}$

2) $\sqrt{8-2x} = x$ $x \geq 0$
 $8-2x = x^2$
 $x^2 + 2x - 8 = 0$
 $(x+4)(x-2) = 0$
 ~~$x = -4$~~ $x = 2$

3) $x = 2\sqrt{3x}$ $x \geq 0$
 $x^2 = 4(3x)$
 $x^2 = 12x$ ✓
 $x^2 - 12x = 0$
 $x(x-12) = 0$
 $x = 0$ $x = 12$

4) $\sqrt{3x+1}+3=x$

$$\sqrt{3x+1} = x-3$$

$$x-3 \geq 0$$

$$3x+1 = x^2 - 6x + 9$$

$$x \geq 3$$

$$0 = x^2 - 9x + 8$$

$$0 = (x-1)(x-8)$$

$$x=1 \quad x=8$$

Use the substitution method:

5) $\sqrt{x}+3\sqrt{x}=0$

$$x+3\sqrt{x}=0$$

$$y^2+3y=0$$

$$y(y+3)=0$$

$$y=0 \quad y=-3$$

$$\sqrt{x}=0 \quad \sqrt{x}=-3$$

$$x=0$$

let $y = \sqrt{x}$
 $y^2 = x$

6) $2\sqrt{x}-3\sqrt[4]{x}-1=0$

let $y = \sqrt[4]{x} = x^{1/4}$
 $y^2 = \sqrt{x} = x^{1/2}$

$$2y^2-3y-1=0$$

$$a=2 \quad b=-3 \quad c=-1$$

$$y = \frac{3 \pm \sqrt{9-4(2)(-1)}}{4} = \frac{3 \pm \sqrt{17}}{4}$$

$$\sqrt[4]{x} = \frac{3 \pm \sqrt{17}}{4}$$

$$x = \left(\frac{3 \pm \sqrt{17}}{4} \right)^4$$

HOMEWORK:
 Equations in Quadratic Form, Part B 17-29 (odd)
 Equations Involving Radicals: 1-16